



Dane: a, α Szukane: $V = \frac{1}{3} P_p \cdot h$, $P_B = 3 \cdot P_{\Delta ABC}$

$$H/a = \sin 60 \quad \text{wiece} \quad H = \frac{a\sqrt{3}}{2} \quad 2/3 H = \frac{a\sqrt{3}}{3}$$

$$h/\frac{a\sqrt{3}}{3} = \operatorname{tg} \alpha \quad \text{wiece} \quad h = \operatorname{tg} \alpha \cdot \frac{a\sqrt{3}}{3}$$

$$P_p = \frac{1}{2} a \cdot H = \frac{1}{2} a \cdot \frac{a\sqrt{3}}{2} = \frac{a^2\sqrt{3}}{4} \quad V = \frac{1}{3} \cdot \frac{a^2\sqrt{3}}{4} \cdot \operatorname{tg} \alpha \cdot \frac{a\sqrt{3}}{3} = \frac{a^3 \operatorname{tg} \alpha}{12}$$

$$P_{\Delta ABC} = \frac{aX}{2}, \quad X^2 = H^2/9 + h^2 \quad \text{skad} \quad X^2 = a^2/12 + 3a^2 \operatorname{tg}^2 \alpha / 9 = \frac{a^2(1+4\operatorname{tg}^2 \alpha)}{12}$$

$$X = \frac{a\sqrt{1+4\operatorname{tg}^2 \alpha}}{2\sqrt{3}} \quad P_{\Delta ABC} = 1/2 \cdot a \cdot X = \frac{a^2}{4\sqrt{3}} \sqrt{1+4\operatorname{tg}^2 \alpha}$$

$$P_B = 3P_{\Delta ABC} = 3 \cdot \frac{a^2}{4\sqrt{3}} \sqrt{1+4\operatorname{tg}^2 \alpha}$$